

# Labor Economics and Employment Policies

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## Lecture 3: Matching, growth, unemployment and wages

- Importance of the magnitude of job creation, job destruction, and worker flows
- Unemployment
- Analyze the functioning of the labor market as a matching process between employers and employees
- Analyze the relation between growth and unemployment
- Think about the efficiency of a labor market with frictions
- Analyze the consequences of the minimum wage

- Christopher Pissarides *Equilibrium unemployment theory*, MIT Press, 2000

# 1. The matching model

- Simple model of the labor market in which transaction costs explain the simultaneous existence of vacant jobs and unemployed persons.
- The model is structured around the concept of “*matching function*,” which sums up, at the aggregate level, the outcomes of encounters between persons in search of a job and firms with positions vacant.
- The matching function,  $V$  vacant jobs,  $U$  unemployed workers  
number of matches per unit of time  $M(V, U)$
- $M$  is increasing with  $V$  and  $U$ .
- $M(V, 0) = M(0, D) = 0$ .
- Constant returns to scale

- The probability of filling a vacant job per unit of time:

$$\frac{M(V, U)}{V} = M(1, U/V) \equiv m(\theta); \quad \theta \equiv V/U \quad (1)$$

Parameter  $\theta$ , which equals the ratio of the number of vacant jobs to the number of unemployed persons, is an indicator of the “tightness” prevailing in the labor market.

- The probability of filling a vacant job decreases with  $\theta$
- For an unemployed person, the probability to find a job is

$$\frac{M(V, U)}{U} = \frac{V}{U} \frac{M(V, U)}{V} = \theta m(\theta) \quad (2)$$

increases with  $\theta$ .

## *Equilibrium of flows and the Beveridge curve*

- Job destruction rate  $q$
- Let  $N_t$  denote the size of the labor force at date  $t$ ,  $N_t \geq N_{t-1}$
- Unemployment rate at date  $t$

$$U_t = U_{t-1} + N_t - N_{t-1} + qL_{t-1} - \theta_{t-1}m(\theta_{t-1})U_{t-1} \quad (3)$$

- Let denote  $u_t = U_t/N_t$  the unemployment rate, and  $n = (N_t - N_{t-1})/N_{t-1}$ ,

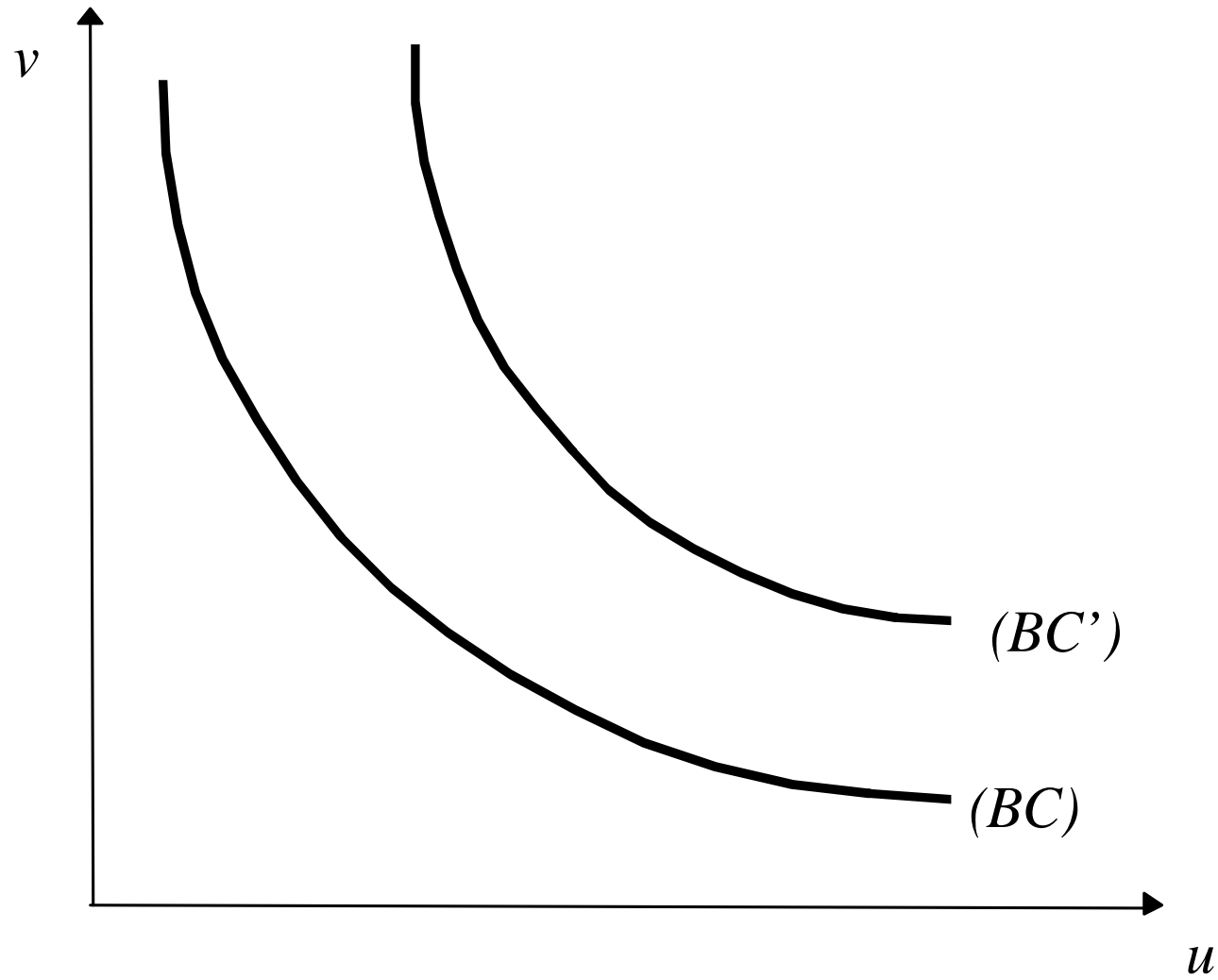
$$u_t(1 + n) = u_{t-1} + q + n - [q + \theta_{t-1}m(\theta_{t-1})]u_{t-1} \quad (4)$$

- The stationary value of the unemployment rate corresponds to  $u_t = u_{t-1}$

$$u = \frac{q + n}{q + n + \theta m(\theta)} \quad (5)$$

- If we define the vacancy rate by  $v = V/N$ , the labor market tightness  $\theta$  is also equal to the ratio  $v/u$ .
- In the plane  $(v, u)$ , this relationship yields the Beveridge curve.

- The Beveridge curve



## *The behavior of firms*

- There are only two goods in the economy: a good produced by the firms and consumed by all individuals; and labor, assumed to be homogeneous, which is the sole factor of production.
- The good produced by the firms is the numeraire.
- Each firm has one job that can be either vacant or filled;
- when this job is filled, It makes possible the production of an exogenous quantity  $y$  of the good per unit of time
- $w$  denotes the wage.
- When it is filled, a job yields an expected profit  $\Pi_e$  which is different from the profit expected  $\Pi_v$  when the job falls vacant.



*The profit expected from a filled job*

$$\Pi_e = \frac{1}{1+r} [(y-w) + q\Pi_v + (1-q)\Pi_e] \quad (6)$$

- Can be rewritten in simpler form:

$$r\Pi_e = y - w + q(\Pi_v - \Pi_e) \quad (7)$$

*The profit expected from a vacant job*

- The costs of a vacant job per unit of time are denoted by  $h$ .
- These costs represent the expenses incurred in holding the position open and looking for an employee with the right skills to fill it (advertising, agency fees, the services of a consultant, etc.).
- Since vacant jobs are filled at rate  $m(\theta)$ , the profit expected from a vacant job is written:

$$\Pi_v = \frac{1}{1+r} \{-h + m(\theta)\Pi_e + [1 - m(\theta)] \Pi_v\}$$

- Or again, rearranging the terms of this relation:

$$r\Pi_v = -h + m(\theta)(\Pi_e - \Pi_v) \tag{8}$$

## *Labor demand*

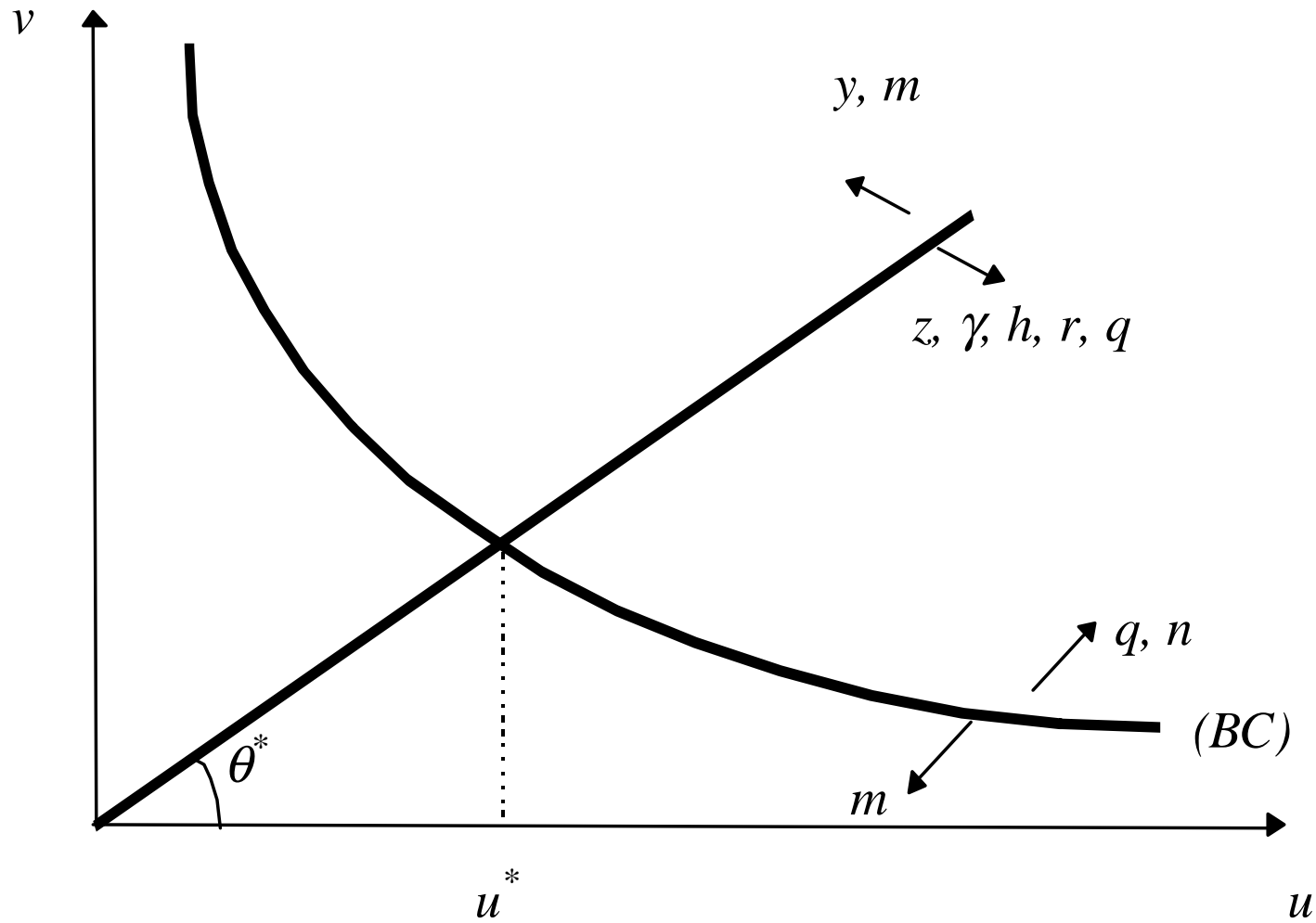
- *free entry* condition; it is written simply  $\Pi_v = 0$ .

- Yields:

$$\frac{h}{m(\theta)} = \frac{y - w}{r + q} \quad (9)$$

- The left hand side of this equation represents the average cost of a vacant job.
- At free entry equilibrium, the average cost of a vacant job must be equal to the profit expected from a filled job.
- Since the rate  $m(\theta)$  at which vacant jobs are filled decreases with the labor market tightness  $\theta$ , equation (9) defines a decreasing relation between the wage and the labor market tightness.

- Labor market equilibrium



## *Properties of the model*

- The growth of the labor force: a rise in the *growth rate*  $n$  of the labor force shifts the Beveridge curve upward
- A rise in productivity  $y$  shifts the labor demand upward.
- A rise in wage  $w$  shifts the labor demand downward
- The efficiency of the matching process
- The job destruction rate
- The interest rate

## *Wage determination*

- The wage depends on
  - productivity
  - the reservation wage
  - income of unemployed workers  $z$
- The wage reads

$$z \leq w(\theta, y) < y$$

increases with  $\theta$  and with  $y$ .

Equilibrium value of the labor market tightness

$$\frac{h}{m(\theta)} = \frac{y - w(\theta, y)}{r + q} \tag{10}$$

## *Labor market efficiency*

- Efficient value of vacancies: maximize output per worker net of vacancy costs

$$\Omega = y(1 - u) + uz - vh$$

- Trade off
  - increase in  $v$ : marginal cost of vacancy:  $h$
  - marginal gain of vacancy: decrease in  $u$
- There exists an optimal level of unemployment which is strictly positive
- Unemployment is useful !